

"Most" Real Numbers Between Zero and One

Have All Ten digits In their Decimal Representation

Let M_0 denote the set of real numbers between zero and one that contain no zero in their decimal. Having no zero in the tenth position eliminates $\frac{1}{10}$ of all reals between zero and one. This leaves all decimals of the form .1ddd...; .2ddd...; .3ddd...; through .9ddd...

Eliminating numbers with zero in the hundredth position will take out $\frac{1}{10}$ of the remaining decimals, so we have $\frac{9}{10}$ of $\frac{9}{10} = \frac{81}{100}$ of the decimals remaining.

Continuing these "cuts" M_0 will have only $\left(\frac{9}{10}\right)^N$ (as N increases without bound) numbers remaining... or to the nearest per cent $\rightarrow 0\%$

Similarly let M_1 denote the set of numbers that don't contain the digit 1. Similarly define M_2 through M_9 . Using the same logic as discussed for M_0 it follows that each of these sets contain "approximately" zero percent of the reals between zero and one.

Let S be the set of real numbers between zero and one that remain after $M_0, M_1, M_2, \dots, M_9$ are removed from the interval. It follows that S contains "nearly" 100% of the interval.

Example .1234567890ddd... is in S because it was not in M_0, M_1, \dots etc. Also $\frac{1}{17}$ is in S . I'll let you check that!